

Medical image Edge detection using Gauss Gradient operator

S.N Kumar^{*1}, A. Lenin Fred², Ajay Kumar H³, Sebastin Varghese⁴

¹Research Scholar, Dept of ECE, Sathyabama University, Chennai – 600119, Tamil Nadu, India.

²School of CSE, Mar Ephraem College of Engineering and Technology, Elavuvilai – 629171, Marthandam, Tamil Nadu, India.

³School of ECE, Mar Ephraem College of Engineering and Technology, Elavuvilai – 629171, Marthandam, Tamil Nadu, India.

⁴Consultant Radiologist, Metro Scans & Laboratory, Trivandrum - 695011, Kerala, India

Abstract

Image segmentation is the process of extraction of desired region of interest and plays a vital role in medical images for the analysis of anatomical organs and anomalies like tumor, cyst. The edge represents the contour of an object and it is the boundary between object and background. In this paper, gauss gradient edge detector was proposed that produces superior results than conventional edge detectors like Sobel, Perwitt, Roberts, Canny and LOG algorithm. The boundary detection in noisy images is a crucial task and the proposed edge detector employs Gaussian filter that generates edges in the efficient manner. The algorithms were tested on abdomen CT images and for validation in terms of PSNR, MSE the benchmark images from Berkeley database were used. The Berkeley database provides gold standard images for evaluation and the algorithms were developed in Matlab2010a.

Key words: Edge detection, Gauss Gradient, Image Smoothing, Mask, Segmentation.

INTRODUCTION

The image comprises of pixel with varying gray level intensity and edges determine the discontinuity in image intensity from one pixel to another. Edge detection techniques are perhaps the traditional techniques to trace the contour of region of interest. Edge detection is the process of determining and locating sharp discontinuities in an image. The edge detection algorithms are designed to respond to sharp edges which can be caused by noisy pixels. In image analysis edge detection plays an important role and it is one of the traditional segmentation technique. The Gaussian filter plays a vital role in edge detectors to produce the refined result. The Gaussian filter was used for 1D signal smoothing and when moved from a fine-to-coarse scale, the zero crossings disappear in scale representation of their second order derivatives and new ones are not created. For 2D signals applications also, zero crossings are not created as the scale increases [1]. Jagadish H. Pujar et al proposed a medical image segmentation model comprising of edge detection by canny and normalized cut eigen vectors. Initially before edge detection, the pre-processing was done by Median, Gaussian or Frost filter based on the type of noise [2]. Gautam Appasaheb Kudale et al proposed that canny edge detector produces good boundary detection in X-ray images and Zero crossings operator, LOG operator also generates satisfactory results [3]. Krit Somkantha et al developed an edge detection technique for medical images to trace the boundaries of anatomical organs based on intensity gradient and texture gradient features; the proposed model produces efficient results when compared with conventional active contour models [4]. Nadeem Mahmood et al applied various edge detection techniques on knee joint articular cartilage MR images; the canny edge detector produces superior results [5]. Jamil A. M. Saif et al used various gradient-based edge detectors on MR and endoscopic images; the canny produces good result, however the tuning of parameters are

required in some cases [6]. Zhao Yu-qian et al proved that morphology edge detector produces efficient result for lung CT images in the presence of noise when compared with the LOG and Sobel edge detector [7]. Emhimed Saffor et al proposed edge detection based on morphological operations on CT images of brain and chest. The edges were determined by taking the difference between the dilated and eroded images [8]. Ed-Edily Mohd. Azhari et al used canny edge detector for the tumor boundary detection on MR images of brain, the edge detectors are often used in hybrid segmentation approaches [9]. Mohamed Abo-Zahhad et al performed an analysis of various edge detection operators on Berkeley data set images and pre-processing by Gaussian filter prior to edge detection produce superior results [10].

RELATED WORK

The most of the edge detection algorithms are based on the derivatives or gradient of the image. The medical images from the acquisition system are susceptible to noise. In general, CT images are corrupted by Gaussian noise, MR images are corrupted by rician noise and US images are affected by speckle noise. In medical images, an edge detection algorithm plays a vital role in the delineation of anatomical organs and pathological issues like tumor or cyst.

The objective of edge detector is to trace the boundary or contour of desired region of interest in the medical image.

The gradient of 2D function $g(x, y)$ is as follows

$$\nabla g = \begin{pmatrix} f_x \\ f_y \end{pmatrix} = \begin{pmatrix} \frac{\partial g}{\partial x} \\ \frac{\partial g}{\partial y} \end{pmatrix}$$

The edge strength is given by the magnitude of the above vector which is represented as below

$$\nabla g = \text{mag}(\nabla g) = (f_x^2 + f_y^2)^{\frac{1}{2}}$$
$$\nabla g = \left(\left(\frac{\partial g}{\partial x} \right)^2 + \left(\frac{\partial g}{\partial y} \right)^2 \right)^{\frac{1}{2}}$$

The gradient direction is determined as follows

$$\theta = \tan^{-1}\left(\frac{f_y}{f_x}\right)$$

The edge detection algorithm should track the edges carefully and false edges due to noisy pixels have to be eliminated. The following are the assumptions made in the edge tracing of images.

- The gradient of edge pixels are stronger and greater than noisy pixels
- The edge magnitude and orientation varies slowly along the edges.

The Sobel operator comprises of a pair of 3×3 convolution kernels as shown in Figure 1. The kernels in the sobel operator produce maximum value to edges running vertically and horizontally. The kernels are applied individually in the input image to produce distinct measurements of the gradient component in each orientation (G_x and G_y). The kernel response are then combined together to find the absolute magnitude of the gradient at each point and the orientation of that gradient [5].

The gradient magnitude is given by:

$$|G| = \sqrt{G_x^2 + G_y^2}$$

Typically, an approximate magnitude is computed using; $|G| = |G_x| + |G_y|$, which is much faster to compute.

The angle of orientation of the edge (relative to the pixel grid) giving rise to the spatial gradient is given by

$$\theta = \arctan\left(\frac{G_y}{G_x}\right)$$

The Sobel edge detection mask to determine the gradient in the x (vertical) and y (horizontal) directions is given below.

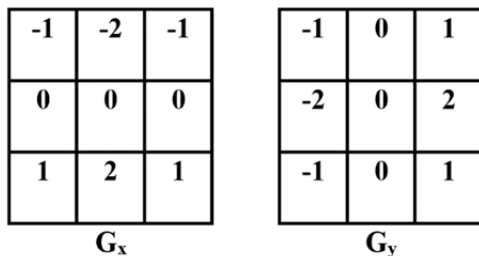


Figure 1. Masks for Sobel edge detector

The Roberts Cross gradient operator is simple and fast to compute, 2-D spatial gradient measurement on an image. The kernels in the Roberts operator produce maximum value to edges running at 45°.

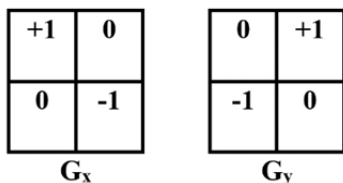


Figure 2. Masks for Robert operator

The Prewitt operator is analogous to the Sobel operator and is used for detecting vertical and horizontal edges in images. Unlike Sobel operator, it does not give importance to pixels closer to the center of the masks.

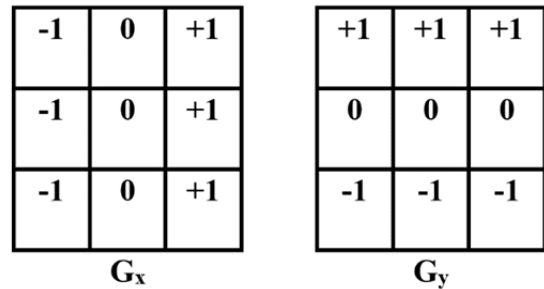


Figure 3. Masks for the Prewitt gradient edge detector
The Laplacian operator is based on second derivative of the image to find edges and searches for zero crossings. The Laplacian $L(x, y)$ of an image with pixel intensity values $I(x, y)$ is represented as follows.

$$L(x, y) = \frac{\partial^2 I}{\partial x^2} + \frac{\partial^2 I}{\partial y^2}$$

The Gaussian smoothing operation is performed initially to make it insensitive to noise. The commonly used kernels in LOG operator are as follows.

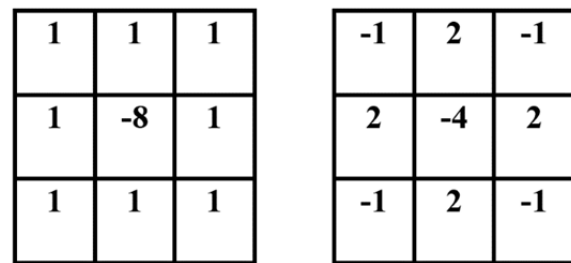


Figure 4. Masks for the Laplacian of Gaussian (LOG) operator

The canny edge detection comprises of two stages edge enhancement and tracking. The Gaussian filter is applied to smooth the image, the larger kernel size lowers the sensitivity to noise. The Sobel edge detection operator is applied to determine the magnitude and direction of the edges. After the edge orientation is determined, non-maximum suppression is applied to trace the path of edge and neglect those pixels that are not the part of the edge. Finally, hysteresis thresholding is applied to eliminate streaking. The two threshold values (t_1 and t_2) with $t_1 > t_2$ are defined and applied to the gradient magnitude of the image. The pixels whose threshold value greater than t_1 are considered as edge pixels and the pixels that are connected to edge pixels greater than t_2 are presumed as edge pixels.

EDGE DETECTION USING GAUSS GRADIENT OPERATOR

The gauss gradient determines the gradient/derivative of the scalar 2D images and 3D volumes using derivatives of Gaussian approach.

The Gaussian kernel in two dimensions is as follows

$$h(x, y) = \frac{1}{2\pi\sigma^2} e^{-\frac{(x^2+y^2)}{\sigma^2}}$$

The term σ in the Gaussian filter is called scale of smoothing. The scale has substantial effect on the response of Gaussian filter. The larger the value of σ , the image will become blurred and sensitivity to noise decreases.

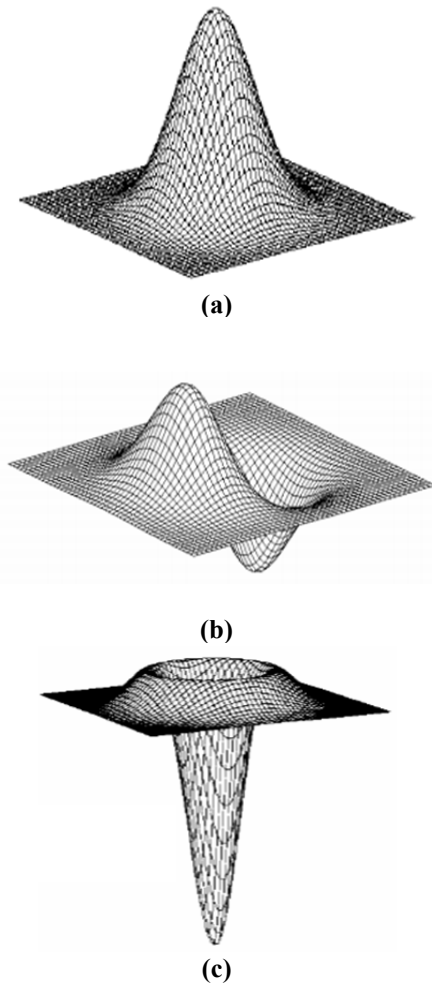


Figure 5. (a) Gaussian function (b) Derivative of Gaussian function (c) Laplacian of Gaussian function

In general, a function $f(x, y)$ in terms of the tensor product is written as follows

$$f(x, y) = g(x)h(y)$$

Here instead of applying the 2D kernel, a separable filtering approach is used to calculate the gradient along x and y direction by 1D kernel.

The Gaussian function is separable and can be decomposed into product of two 1 D Gaussian functions.

$$f(x, y) = \left(\frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{x^2}{2\sigma^2}} \right) \left(\frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{y^2}{2\sigma^2}} \right)$$

The important property of the Gaussian filter is the only filter that satisfies the uncertainty relation.

$$\Delta x \Delta w \geq 1/2$$

Where Δx and Δw are the variance in spatial and frequency domain respectively. The unique property gives the best tradeoff between the conflicting goals of the localization in spatial and frequency domain respectively. For a filter, the tensor products are called the separable kernel. The response of Gaussian kernel is non-zero over an infinite domain and for most of the domain; it is very small because of the exponential form.

The steps in gauss gradient edge detection are summarized as follows

Step 1: The input image can be gray scale or color image. The term sigma is used to determine the Gaussian kernel

along both directions. The higher value of sigma will blur the resultant output. Choose appropriate value of sigma in gauss gradient edge detection approach.

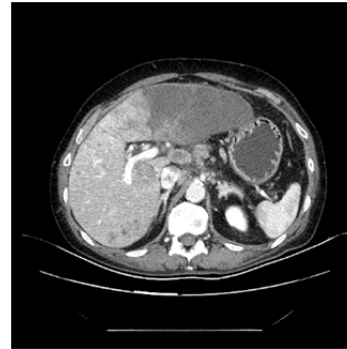


Figure 6. Input Dicom medical image

Step 2: The Gaussian kernel is generated along the x and y direction. The Gaussian kernel generated involves the convolution of Gaussian function and first order derivative of Gaussian function.

$$g(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{x^2}{2\sigma^2}}$$

The first order derivative of gaussian function is expressed as follows

$$\frac{\partial}{\partial x} (g(x)) = \frac{1}{\sigma\sqrt{2\pi}} \frac{-2x}{2\sigma^2} e^{-\frac{x^2}{2\sigma^2}}$$

$$g'(x) = -x \left(\frac{1}{\sigma\sqrt{2\pi}} \right) \frac{e^{-x^2}}{2\sigma^2} * \frac{1}{\sigma^2}$$

$$g'(x) = -x * g(x) * \sigma^2$$

The Gaussian kernels along x and y direction are represented as follows.

$$H_x = g(x) * g'(x) \text{ and } H_y = H_x'$$

0.0012	0.0041	0.0083	0.0081	0	-0.0081	-0.0083	-0.0041	-0.0012
0.0055	0.0195	0.0395	0.0384	0	-0.0384	-0.0395	-0.0195	-0.0055
0.0167	0.0592	0.1199	0.1168	0	-0.1168	-0.1199	-0.0592	-0.0167
0.0324	0.1153	0.2335	0.2274	0	-0.2274	-0.2335	-0.1153	-0.0324
0.0405	0.1440	0.2916	0.2840	0	-0.2840	-0.2916	-0.1440	-0.0405
0.0324	0.1153	0.2335	0.2274	0	-0.2274	-0.2335	-0.1153	-0.0324
0.0167	0.0592	0.1199	0.1168	0	-0.1168	-0.1199	-0.0592	-0.0167
0.0055	0.0195	0.0395	0.0384	0	-0.0384	-0.0395	-0.0195	-0.0055
0.0012	0.0041	0.0083	0.0081	0	-0.0081	-0.0083	-0.0041	-0.0012

(a)

0.0012	0.0055	0.0167	0.0324	0.0405	0.0324	0.0167	0.0055	0.0012
0.0041	0.0195	0.0592	0.1153	0.1440	0.1153	0.0592	0.0195	0.0041
0.0083	0.0395	0.1199	0.2335	0.2916	0.2335	0.1199	0.0395	0.0083
0.0081	0.0384	0.1168	0.2274	0.2840	0.2274	0.1168	0.0384	0.0081
0	0	0	0	0	0	0	0	0
-0.0081	-0.0384	-0.1168	-0.2274	-0.2840	-0.2274	-0.1168	-0.0384	-0.0081
-0.0083	-0.0395	-0.1199	-0.2335	-0.2916	-0.2335	-0.1199	-0.0395	-0.0083
-0.0041	-0.0195	-0.0592	-0.1153	-0.1440	-0.1153	-0.0592	-0.0195	-0.0041
-0.0012	-0.0055	-0.0167	-0.0324	-0.0405	-0.0324	-0.0167	-0.0055	-0.0012

(b)

Figure 7. (a) Kernel generated along x direction (H_x), (b) Kernel generated along y direction (H_y)

Step 3: The Gaussian smoothing is performed on the image using the generated kernels and the results are depicted below

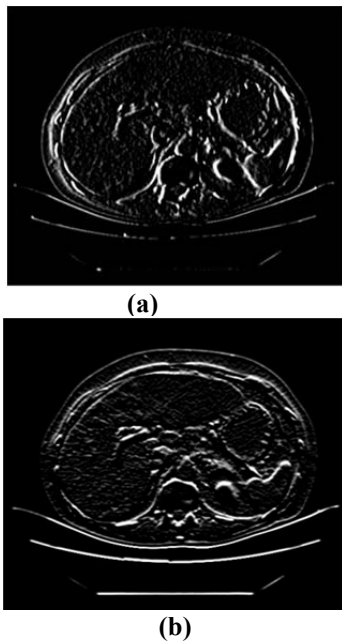


Figure 8. Gaussian kernel response of image along x and y direction

Step 4: The edge detected image is obtained as follows

$$Edge\ output = abs(G_x) + abs(G_y)$$

Where G_x and G_y are gaussian smoothed version of image. The gauss gradient output for $\sigma=1, 1.5$ and 2 are depicted above. From the results, the following inferences can be made. For $\sigma=1$, the resultant output has under segmentation effect, the over segmentation occurs for $\sigma=2$. An optimum value of $\sigma=1.5$ produces efficient result.

RESULTS AND DISCUSSION

In this section to determine the performance of the gauss gradient edge detector, the experiments was carried out on both The Berkeley segmentation dataset (BSD) and real medical images. The proposed gauss gradient edge detector in this paper was compared with the conventional edge detectors. The simulation was done by Matlab 2010a software on the system with the specifications: Intel core i3 @ 3.30 Ghz with 4 GB RAM, Windows 10 operating system running on 64 bit processor.

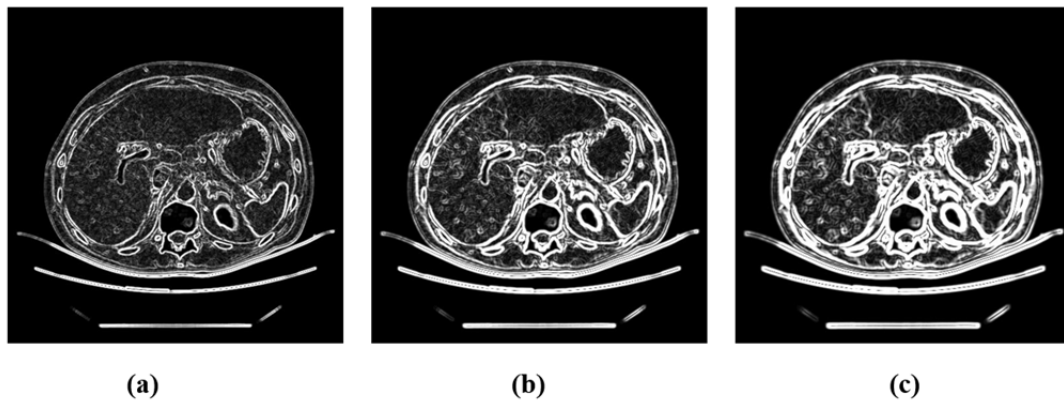


Figure 9. Gauss gradient output for $\sigma= 1, 1.5, 2$.

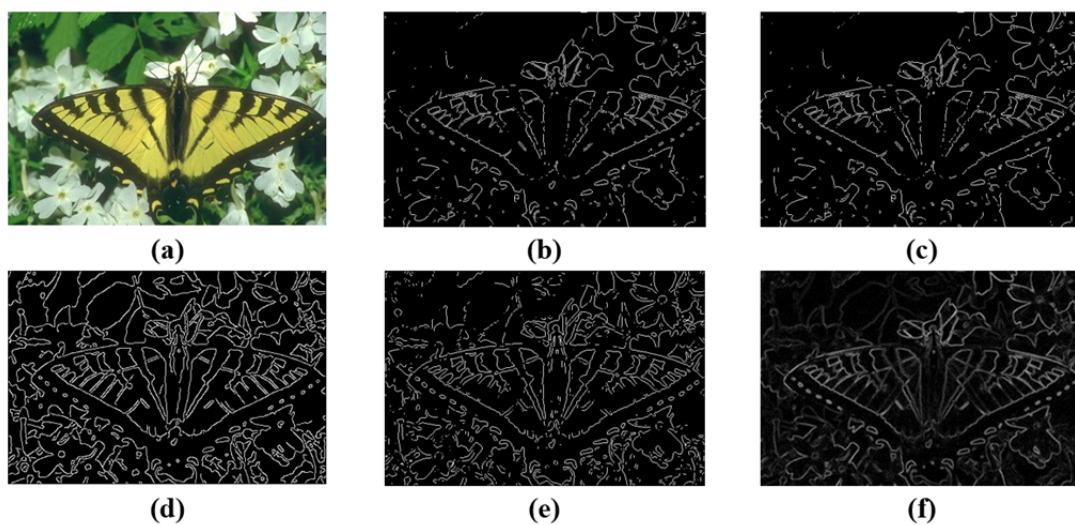


Figure 10. (a) Input image from BSD, (b) Sobel, (c) Prewitt, (d) Canny, (e) Log Operator, (f) Gauss Gradient

The figure 10 above depicts the proposed gauss gradient edge detector output along with the conventional edge detectors. The performance of the proposed algorithm was evaluated by metrics like PSNR and MSE.

$$PSNR = 10 \log_{10} \left(\frac{R^2}{MSE} \right)$$

$$MSE = \frac{\sum_{M,N} [I_I(M,N) - I_O(M,N)]^2}{M,N}$$

Where $I_I(M,N)$ represents the edge detector output and $I_O(M,N)$ represents the ground truth image.

The gauss gradient approach produce efficient result for all the images in the Berkeley segmentation dataset and the

result of selective images are depicted in figure 11. The performance metrics plot in figure 12 reveals that the gauss gradient approach has high PSNR and low MSE. The computation time of the algorithms are depicted in figure 13. The computation time of the gauss gradient approach was slightly higher than the Log, Canny and Prewitt approaches, however in terms of the quality of edge tracing the gauss gradient outperforms the other conventional techniques. For the computation of PSNR and MSE, ground truth images are available in the Berkeley segmentation dataset.

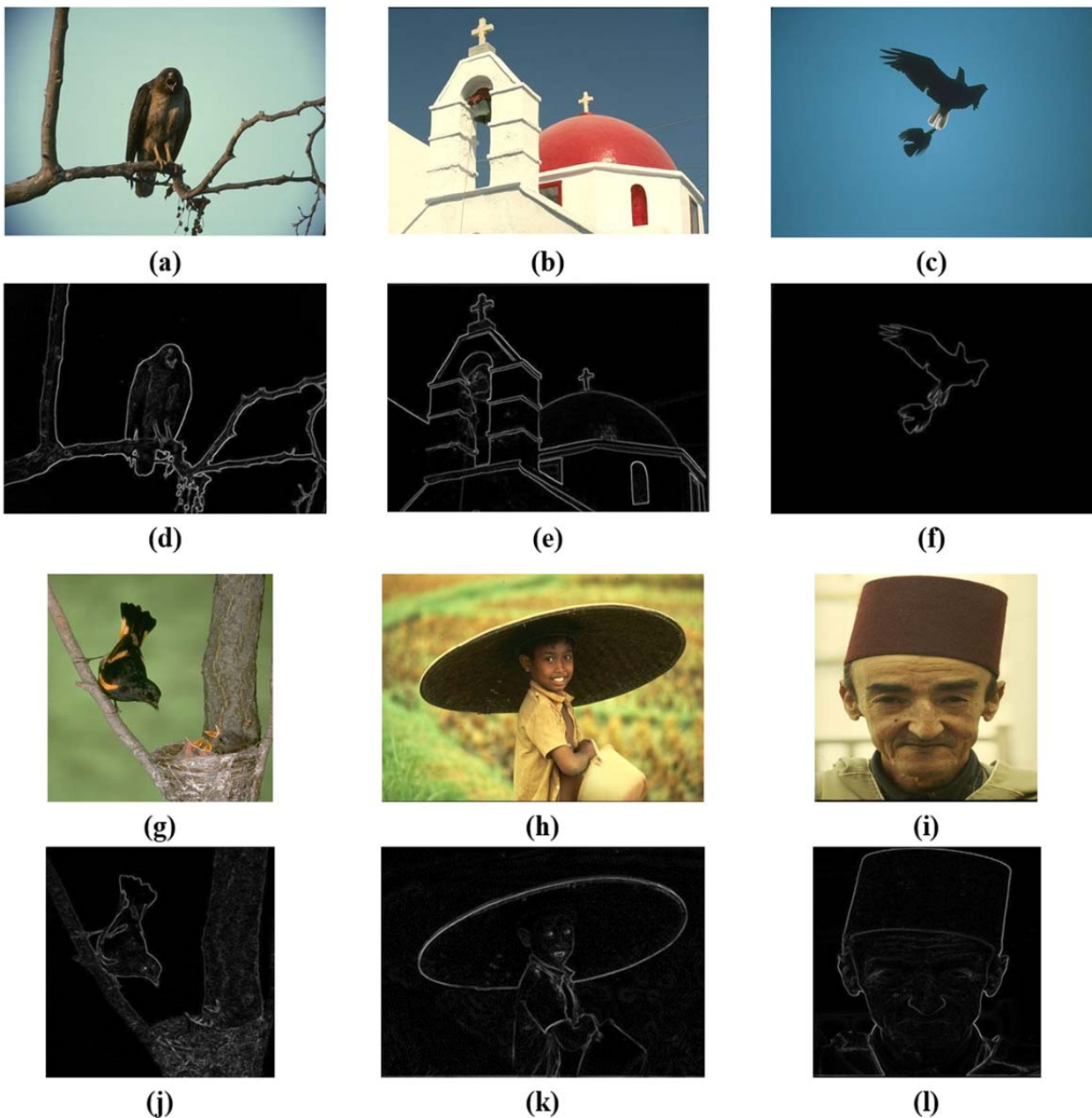


Figure 11. Input images from Berkeley Segmentation Dataset and their corresponding Gauss Gradient edge detected images ($\sigma = 1.5$)

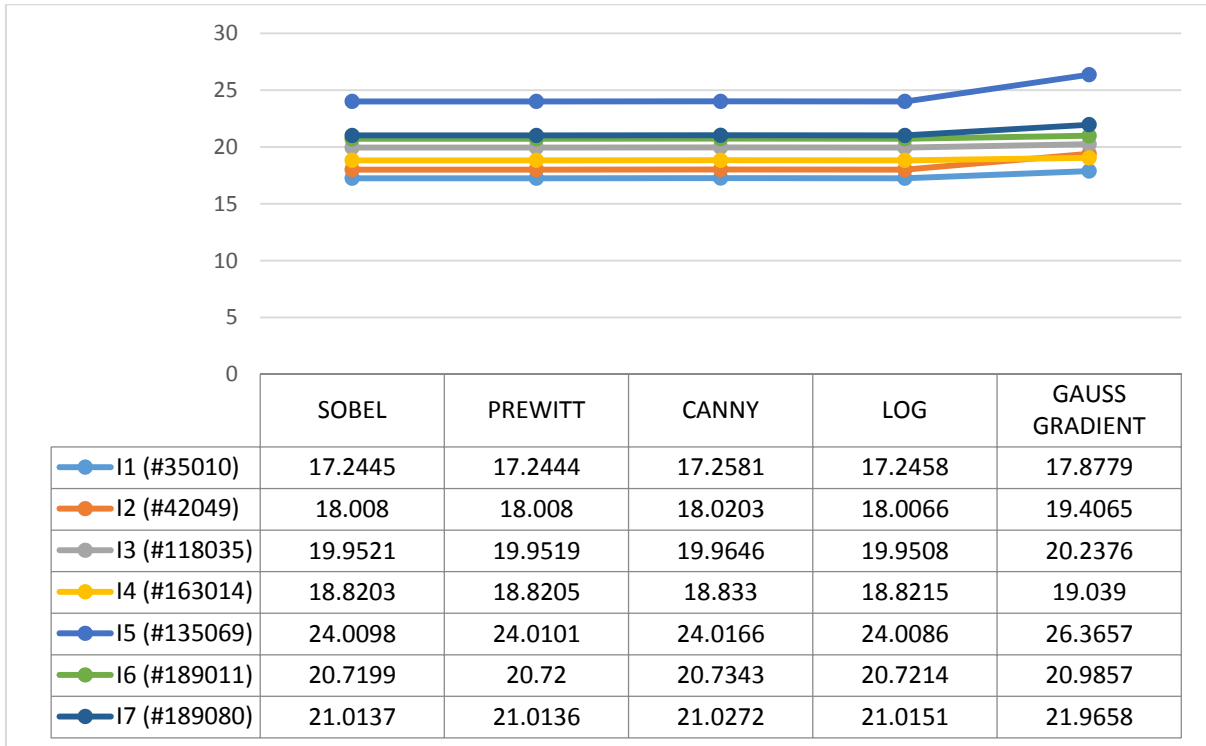


Figure 12. PSNR plot of edge detector algorithms for input images from BSD

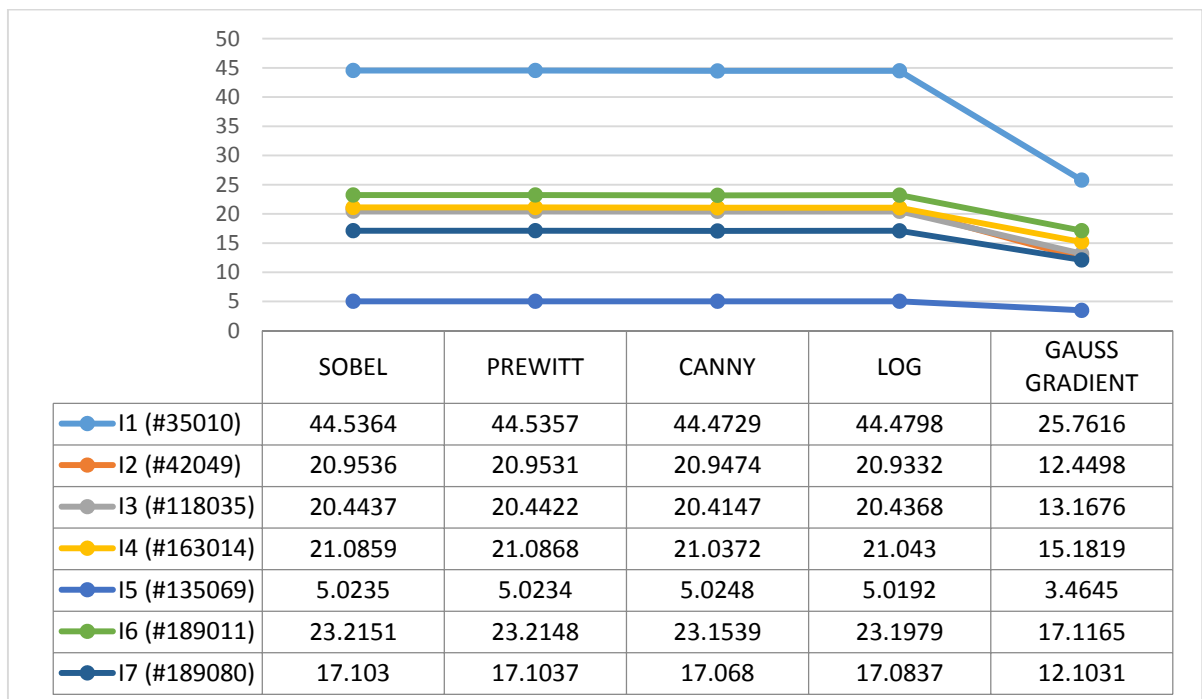


Figure 13. MSE plot of edge detector algorithms for input images from BSD

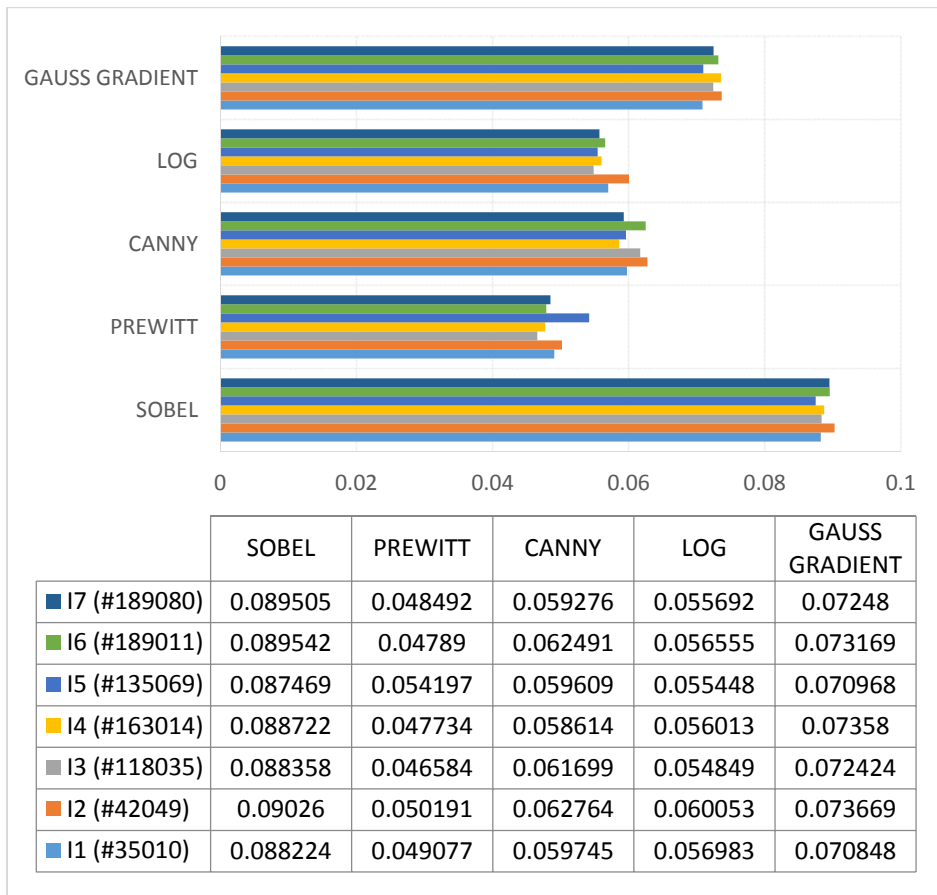


Figure 14. Time plot of edge detector algorithms for input images from BSD

The gauss gradient approach also produces robust result for the real abdomen CT images. The figure 15 represents the edge detection for abdomen CT images of .png format. The computation time is depicted in figure 16.

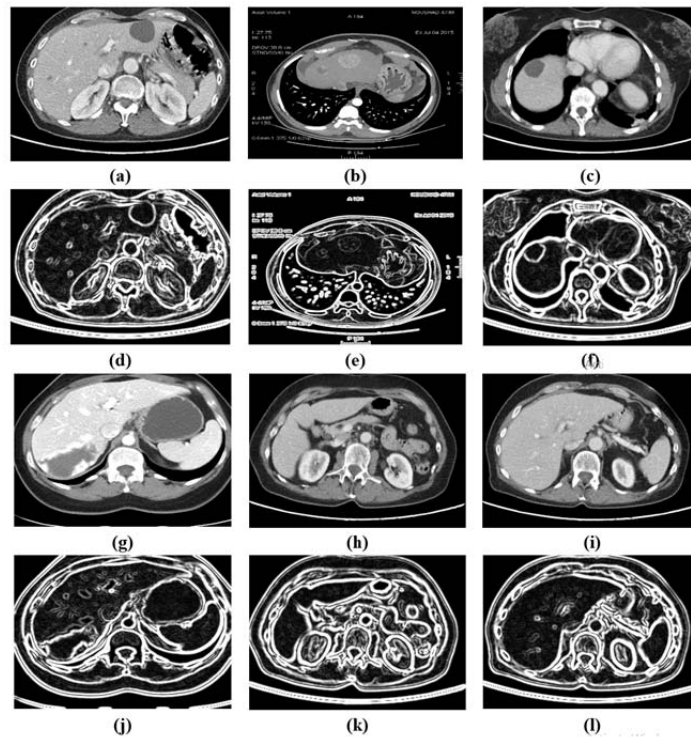


Figure 15. Input images I 8 – I 13 (a,b,c,g,h,i) and their corresponding Gauss Gradient output images (d,e,f,j,k,l)

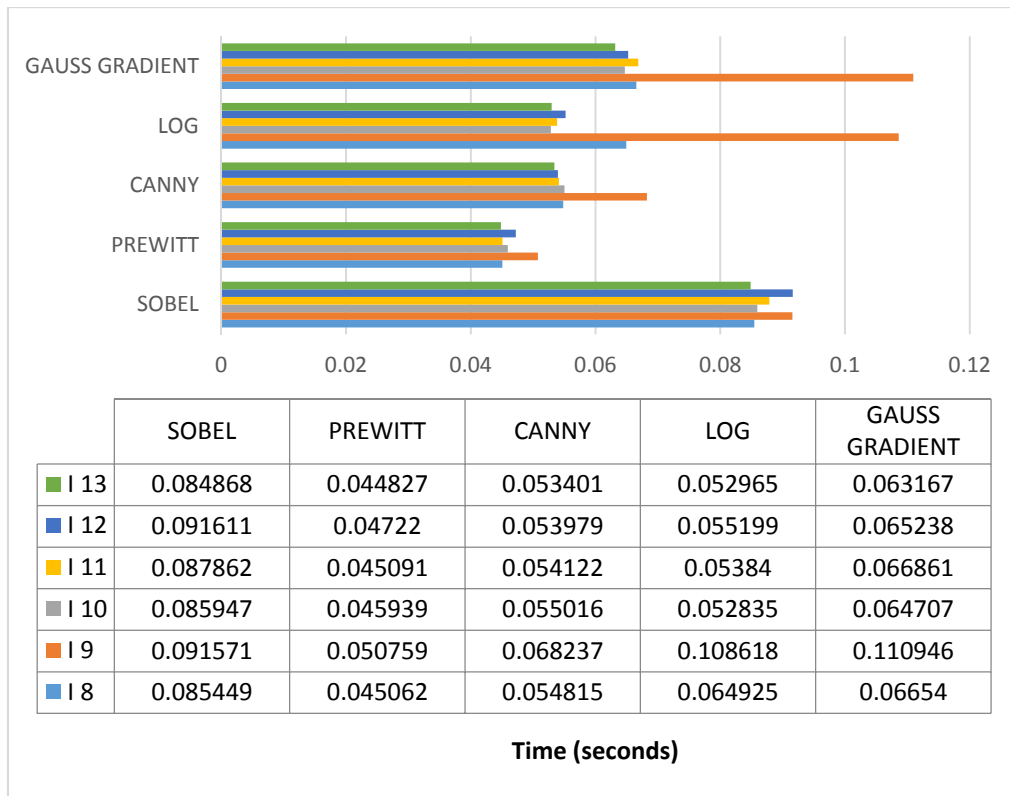


Figure 16. Time Plot of edge detector algorithms for .png format medical images

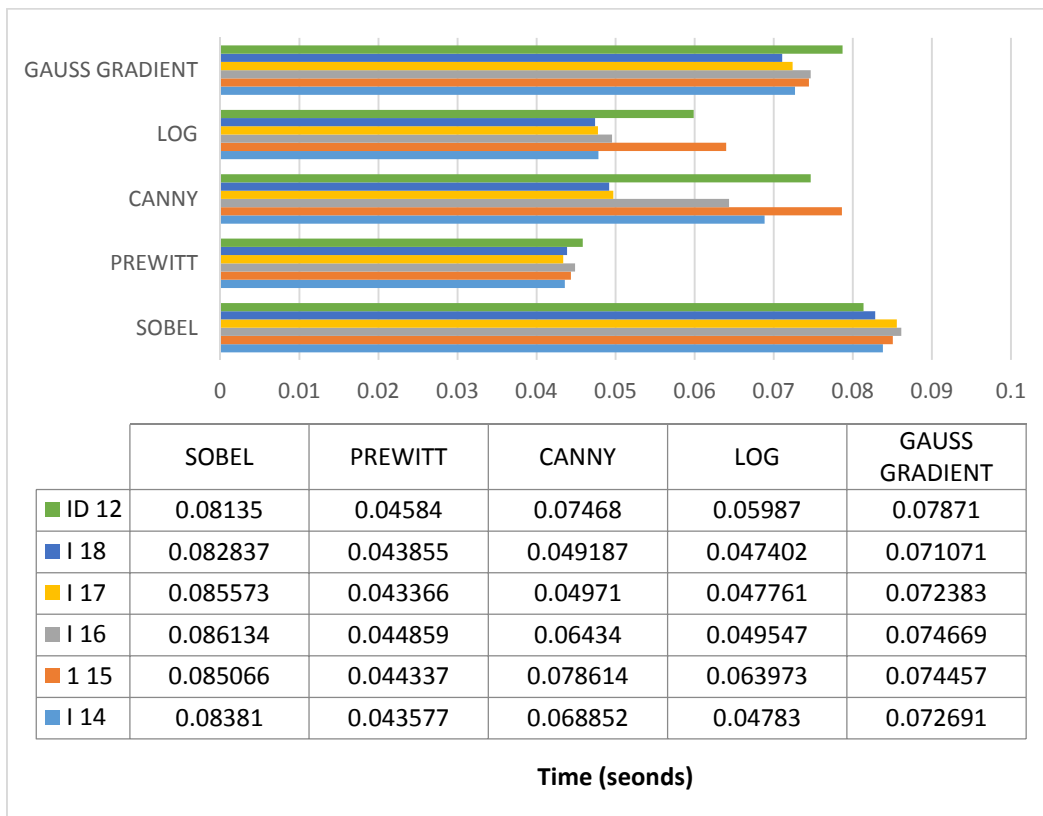


Figure 18. Time Plot of edge detector algorithms for Dicom medical images

The edge detection techniques were also tested on medical Dicom abdomen CT images and the results are depicted below. The computation time is depicted in figure 18.

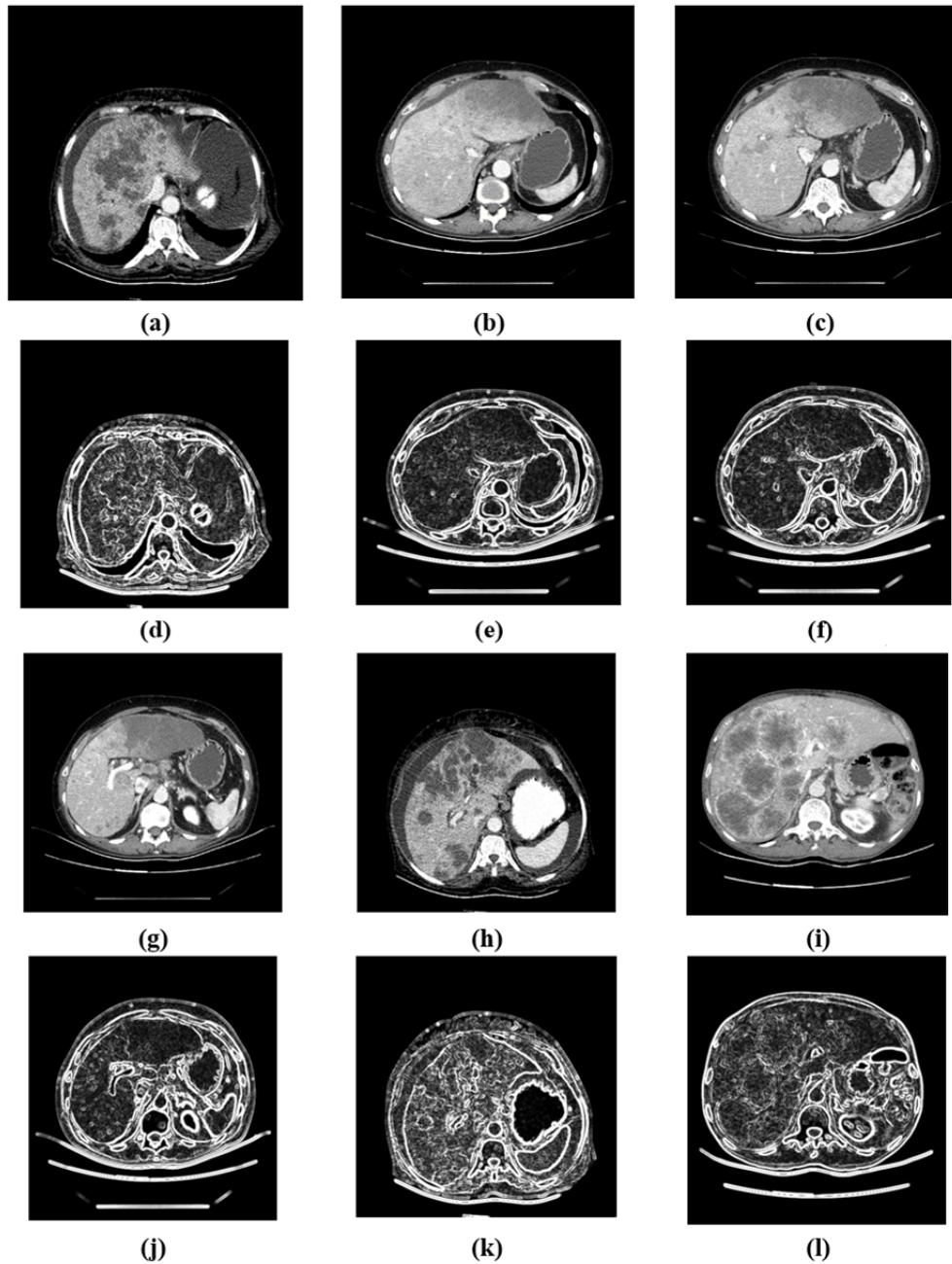


Figure 17. Dicom input images I 14 – I 19 (a,b,c, g, h, i) and their corresponding Gauss Gradient output images (d,e,f,j,k,l)

CONCLUSION

This paper proposes gauss gradient technique for edge detection and satisfactory results were produced when compared with the conventional edge detectors. The algorithm works well on images from Berkeley segmentation dataset and real abdomen CT Dicom images. The PSNR and MSE for Berkeley segmentation dataset images show the superiority of gauss gradient approach with the conventional edge tracer algorithms. The computation time is slightly higher than the conventional edge detectors, however the quality of edge detection is greatly improved. The segmentation plays a vital role in

telemedicine applications for the analysis of region of interest. The significance of this work is that, the proposed algorithm can be an effective aid for telemedicine applications.

ACKNOWLEDGEMENT

The authors would like to acknowledge the support provided by DST under IDP scheme (No: IDP/MED/03/2015). We thank Dr. Sebastian Varghese (Consultant Radiologist, Metro Scans & Laboratory, Trivandrum) for providing the medical CT images and supporting us in the preparation of manuscript.

REFERENCE

- [1]. Mitra Basu, Gaussian-Based Edge-Detection Methods—A Survey, *IEEE Trans. on Systems, Man, and Cybernetics—Part C: Applications and Reviews*, 2002, 32 (3), 252- 260.
- [2]. Jagadish H. P, Pallavi S. G, Shambhavi D. S, Kiran S. K, Medical Image Segmentation based on Vigorous Smoothing and Edge Detection Ideology, *International Journal of Electrical, Computer, Energetic, Electronic and Communication Engineering* 2010, 4 (8), 1143 – 1149.
- [3]. Gautam A K, Mahesh D. P, Study and Analysis of Various Edge Detection Methods for X-Ray Images, *Int J Computer Sci Appl.*, 2010, 2010, 15-17.
- [4]. K Somkantha, Nipon T-U, Sansanee A, Boundary Detection in Medical Images Using Edge Following Algorithm Based on Intensity Gradient and Texture Gradient Features, *IEEE Transactions On Biomedical Engineering*, 2011, 58 (3), 567 – 573.
- [5]. Nadeem M, Asadullah S, A Waqas, Adamu A, S Kamran, S B Zaidi, Image Segmentation Methods and Edge Detection: An Application to Knee Joint Articular Cartilage Edge Detection, *Journal of Theoretical and App. Info. Tech.*, 2015, 71 (1), 87 -96.
- [6]. Jamil A. M. Saif, Mahgoub H. Hammad, and Ibrahim A. A. Alqubati, Gradient Based Image Edge Detection, *IACSIT International Journal of Engineering and Technology*, 2016, 8 (3), 153 – 156.
- [7]. Zhao Yu-qian, Gui Wei-hua, Chen Zhen-cheng, Tang Jing-tian, Li Ling-yun, Medical Images Edge Detection Based on Mathematical Morphology, In *2005 IEEE Engineering in Medicine and Biology 27th Annual Conference*, 2005, 6492-6495.
- [8]. E Saffor and A Salama, Objective Evaluation of Mathematical Morphology Edge Detection on Computed Tomography (CT) Images, *International Journal of Medical, Health, Biomedical, Bioengineering and Pharmaceutical Engineering*, 2013, 7 (9), 584-588.
- [9]. Ed-Edily M. A, M. Mudzakkir M. H, Z Zaw Htike and Shoon Lei Win, Tumor Detection in Medical Imaging: A Survey, *International Journal of Advanced Information Technology*, 2014, 4(1), 21 – 29.
- [10]. M Abo-Zahhad, R R Gharieb, S M. Ahmed, A Abd El-Baset Donkol, Edge Detection with a Preprocessing Approach, *Journal of Signal and Information Processing*, 2014, 5, 123-134.
- [11]. R Maini, Himanshu A, Study and Comparison of Various Image Edge Detection Techniques, *International Journal of Image Processing*, 2009, 3 (1), 1 – 11.
- [12]. D. Martin and C. Fowlkes and D. Tal and J. Malik, A Database of Human Segmented Natural Images and its Application to Evaluating Segmentation Algorithms and Measuring Ecological Statistics, *Proc. 8th Int'l Conf. Computer Vision*, 2001, 2, 416 – 423.